

Business-Driven Management of Hybrid IT Infrastructures

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Abstract

With the emergence of the cloud computing paradigm and the continuous search to reduce the cost of running Information Technology (IT) infrastructures, we are currently experiencing an important change in the way these infrastructures are assembled, configured and managed. In this research we consider the problem of managing a hybrid high-performance computing infrastructure whose processing elements are comprised of in-house dedicated machines, virtual machines acquired from cloud computing providers, and remote virtual machines made available by a best-effort peer-to-peer (P2P) grid. Each of these resources has a different cost basis. The applications that run in this hybrid infrastructure are characterised by a utility function: the utility yielded by the completion of an application depends on the time

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taken to execute it. We take a business-driven approach to managing this infrastructure, aiming to maximise profit, that is, the utility produced as a result of the applications that are run minus the cost of the computing resources that are used to run them. We assume that the cost of computing resources from the local in-house machines is unavoidable, i.e.. the in-house infrastructure has a fixed cost whether or not its resources are used. We also assume that the cost of computing resources from the P2P grid (when they are available) is negligible, because the grid is based on the exchange of spare resources between peers. Applications are run using computing power just from these two sources whenever possible. Any extra capacity required to improve the profitability of the infrastructure is purchased from the cloud computing market. We assume that this extra capacity is reserved for future use through short term contracts which are negotiated without human intervention. The cost per unit of computing resource may vary significantly between contracts, with more urgent contracts normally being more expensive. However, due to the uncertainty inherent in the best-effort grid, it may not be possible to know in advance exactly how much computing resource will be needed from the cloud computing market. Overestimation of the amount of resources required leads to the reservation of more than is necessary; while underestimation leads to the necessity of negotiating additional contracts later on to acquire the remaining required capacity. We propose heuristics to be used by a contract planning agent in order to balance the cost of running the applications and the utility that is achieved with their execution, with the aim of producing a high overall profit. We demonstrate that the ability to estimate the grid behaviour is an important condition for making contracts that produce high efficiency in the use of the hybrid infrastructure. We propose a model for predicting the behaviour of a P2P grid that uses a particular incentive mechanism, and assess the suitability of this model using field data. Our results show that the proposed model is able to predict the grid behaviour with an average error that is not larger than 16% for the scenarios evaluated, leading to a worst case efficiency of 85.32%.

Key words:

cloud computing, grid computing, peer-to-peer, business-driven IT management, capacity planning.

1. Introduction

A new business model is currently being adopted which is changing the way that Information Technology (IT) resources and services are deployed and used. In this model the acquisition of resources and services occurs whenever and wherever needed, and the amount charged is related to the amount of resources and services that are actually used. This model of IT sold as a service has been called *cloud computing*. One of its main selling points is the possibility of substantial reductions on the total cost of ownership of IT infrastructures.

Economic advantages certainly play an important role in the adoption of this business model, but there are other important factors to consider which are likely to result in organisations preserving at least some of their in-house infrastructure, rather than having all their applications run on computers owned by cloud service providers. For example, the retention of some in-house capacity may serve to cushion the effects of price fluctuations given by transient instabilities in the cloud computing market. The migration from services supported by in-house dedicated IT infrastructures to services offered by an external cloud computing provider is likely to face strong resistance from the internal IT management staff. For certain types of application the cost reduction resulting from a move to external providers may be low. Most importantly, organisations may decide that they do not wish to execute certain types of application on a computing infrastructure that they do not own or manage: these might include for example business-critical applications requiring very high availability, or applications that process sensitive data.

The market-based cloud computing model is not the only way to reduce total cost of ownership. Among other solutions proposed, peer-to-peer (P2P) grid computing has been suggested as a way to enable a simpler economy for the trading of computing cycles that would otherwise be idle [1]. Markets rely on the existence and efficiency of contract negotiation, norm enforcement, banking and accounting mechanisms. For several scenarios in distributed computing (and also outside computing), implementing such mechanisms is complex, costly or inefficient. In contrast, sharing systems may be efficient for these scenarios, as they can use information which is loosely structured and therefore easier to obtain, they can make use of social relations for monitoring and enforcement, and they have lower marginal transaction costs [2]. These solutions generally give no guarantees on the quality of service provided – indeed, they do not guarantee that the service will be provided at

38 all. Nevertheless, they have been successfully used to increase the cost effec-
39 tiveness of IT infrastructures in a number of settings [3].

40 We expect that in the near future many IT infrastructures will use both
41 resources provided by in-house dedicated infrastructure and resources from
42 external cloud computing providers. Moreover, spare capacity of the in-
43 house infrastructure may be used to execute workload on behalf of other
44 organisations, in exchange for the possibility of using these organisations'
45 spare capacity to run part of the local workload in the future. The different
46 components of this hybrid infrastructure will provide different guarantees,
47 ranging from potentially very detailed quality of service guarantees, to no
48 guarantees at all for best-effort components.

49 This expectation is supported by our own experience with the OurGrid
50 middleware (<http://www.ourgrid.org/>). This middleware allows the deploy-
51 ment of open P2P grids. We have used the OurGrid middleware to foster the
52 creation of the OurGrid Community, which has been used as a computing
53 platform in a variety of application areas, including engineering, bioinfor-
54 matics, computer science and financial applications [4, 5, 6, 7] (for a current
55 snapshot of the running system, see <http://status.ourgrid.org/>). In particu-
56 lar, OurGrid supports the cooperative work of a community of meteorologists
57 and hydrologists, both in academia and in government [4, 8]. Some members
58 of this community provide daily weather forecasts as a public service (see,
59 for instance, <http://www.cptec.inpe.br/>). The capacity required at critical
60 times (when time-constrained applications are run) is normally much larger
61 than that required at other times. Provisioning the IT infrastructure of these
62 public agencies to cope with the high demand at critical times is not cost-
63 effective. An agency will in general be able to obtain some additional capacity
64 at a negligible cost from OurGrid at such a time; however, since OurGrid
65 is best-effort, the agency cannot rely on OurGrid to always provide the ca-
66 pacity required. In this setting, it is likely that extra computing power that
67 is not obtainable from OurGrid could be purchased on demand from cloud
68 service providers at a smaller cost than the cost of provisioning the agency's
69 in-house dedicated infrastructure to meet such demands. The presence of
70 OurGrid reduces the amount of computing power which an agency will need
71 to purchase at critical times. So, a hybrid IT infrastructure consisting of all
72 three potential sources of computing resources (in-house, an external cloud
73 computing provider, and a P2P grid) is highly desirable for this scenario.

74 Since most studies of IT management have assumed that IT services are
75 provided by just one of these sources, interesting research questions arise

76 from consideration of the hybrid IT environment just described. In contrast
77 to existing work that focuses on the management of the cloud computing
78 provider’s infrastructure (e.g. [9]), in this paper we take the point of view of
79 the customer of a cloud computing service. More precisely, we discuss how
80 this customer (the manager of the hybrid infrastructure) can make the best
81 use of the dedicated in-house capacity, while judiciously using the other two
82 sources of computing resources or services. We concentrate on the *contract*
83 *planning* aspect of the IT infrastructure management [10], i.e., *given a utility*
84 *function for an application and its predicted workload, how should one plan*
85 *the contracts that will be made with cloud computing providers, in order to*
86 *balance the cost of executing the application and the utility yielded by its*
87 *execution?*

88 We study heuristics used by a contract planner agent which follows a
89 business-driven approach to managing this infrastructure, meaning that it
90 aims to maximise profit, where the profit in this case is the utility produced
91 as a result of the applications that are run minus the cost of the comput-
92 ing resources that are used to run them. We assume that the agent does not
93 have any say in which applications are to be run on the hybrid infrastructure,
94 but can choose how much cloud computing capacity to reserve and when to
95 make the reservations. In particular, we extend the work by Maciel Jr. et
96 al. [11] where the hybrid infrastructure described above was first presented,
97 and which highlighted the importance of an accurate prediction of the be-
98 haviour of the P2P grid. Here we extend the model to a larger spectrum
99 of applications, and look more closely at the impact that an error in the
100 prediction of the behaviour of the grid has on the overall efficiency of the
101 system. In this direction, we propose a model for predicting the quality of
102 service offered by a P2P grid that uses the incentive mechanism proposed
103 by Andrade et al. [12], and we evaluate the model using data from the Grid
104 Workload Archive [13].

105 For the applications that we had in mind when writing this paper, the
106 computing resource used from the IT infrastructure is simple processing
107 power. However, our analysis can also be applied to applications which
108 use a different type or resource or service. For the rest of this paper we
109 will write “cycle” as shorthand for a unit of computing services or resources:
110 this could for example be an amount of computing power equivalent to a
111 fixed quantity of CPU cycles on a reference machine when the application
112 considered uses processing power from the infrastructure, or 1KB of storage
113 when the application uses storage from the infrastructure, or one unit of a

114 particular higher-level service. We will assume however that the application
115 only requires one type of service or resource, and is sufficiently parallel that it
116 can use any two cycles from any two sources interchangeably and in parallel.
117 (These assumptions are true for most of the applications that are run using
118 OurGrid.)

119 The remainder of the paper is organised as follows. In Section 2 we survey
120 related work. Section 3 gives formal definitions of the application that we
121 will consider and of the hybrid IT infrastructure. A formal description of the
122 problem we target is given in Section 4. We present heuristics for contract
123 planning in Section 5, and evaluate them in Section 6. In Section 7 we
124 propose and validate the model for predicting the quality of service of the
125 P2P grid. Finally, in Section 8 we give concluding remarks and discuss areas
126 in which further research needs to be developed.

127 2. Related Work

128 In this paper, the applications that we are interested in are ones that are
129 time-constrained. There are many examples of distributed applications in
130 which customers need guarantees on the response time and on the allocation
131 of resources. Examples of the domain areas of these applications include:
132 remote medicine [14]; real-time control of sensitive sites, instruments and
133 air traffic flow [15, 16]; multimedia and stream processing [17, 18]; environ-
134 mental forecast [19, 4]; and e-Science experiments [20, 21]. There have been
135 some efforts to develop real-time support in distributed applications [22, 23],
136 and to improve quality of service guarantees of high-performance distributed
137 computing systems by using *advance reservations* [24, 25, 26]. However, a
138 better understanding of the quality of service requirements of these real-time
139 applications is desirable. As yet there is not a complete understanding of
140 how to generate functions that express the utility that customers gain from
141 their applications given the length of the time that the application takes
142 to complete. However, some work on determining these utility functions has
143 been done under the assumptions that the utility functions are step functions
144 or have a linear decay over time [27, 28, 9, 29]. In our work, we consider
145 three time-constrained applications whose utilities to the customer are a step
146 function, a linearly decaying function, and an exponential decaying function.

147 There are some similarities between our work and that of Popovici and
148 Wilkes [9] and Yu et al. [28], as well as some points in which our work comple-
149 ments these earlier papers. Popovici and Wilkes focus on the operations of a

150 service provider, while Yu et al. look at the interaction between a customer
151 and a grid service provider. Our work, on the other hand, investigates the
152 interaction of a customer with both a best-effort grid and a cloud computing
153 provider.

154 Popovici and Wilkes [9] propose an economics-oriented approach for a
155 service provider, to solve the question of which customers' requests the ser-
156 vice provider should accept. They extend works by Chun and Culler [30]
157 and Irwin et al. [29], by considering a service provider that offers job-based
158 services to its clients and rents resources from a resource provider. The dif-
159 ficulty in selecting the requests is that they assume that the service provider
160 will have some uncertainty about the availability of the resources necessary
161 to fulfil the requests. Popovici and Wilkes define risk-aware heuristics for ad-
162 mission control and scheduling that aim at maximising the service provider's
163 utility, taking into account the uncertainty in resource availability. In our
164 work we consider a contract planner for a hybrid IT infrastructure, and the
165 uncertainty comes from the best-effort nature of the P2P grid.

166 Yu et al. [28] propose a scheduling algorithm that minimises the execution
167 costs of workflows in a grid while meeting users' specified deadlines. The
168 unreliability of the grid introduces uncertainty. This, in turn, is dealt with
169 by re-scheduling tasks that fail, moving them to other available computers in
170 the grid. Predictions of availability and information about the costs of grid
171 resources under available contracts are used to select the most appropriate
172 contracts and to minimise cost. Our work uses a similar strategy, but applies
173 it to a different context.

174 Cloud computing providers require solid business models. Rappa [31]
175 presents a general overview of what the business model for cloud computing
176 might look like, taking account characteristics such as necessity, reliability,
177 usability, and scalability. This model is similar to business models for the
178 provision of utilities such as water, telephone, Internet access, and electricity.
179 The pricing model for cloud computing resources that we use in this paper
180 is based on pricing models used for other utilities, in which there is a charge
181 for the reservation of resources.

182 Buyya et al. provide some economic models for setting the prices of
183 services based on supply and demand. These include commodity markets,
184 posted prices, and auctions [32]. Buyya et al. describe a system architecture
185 and policies for resource management in grid infrastructures, based on the
186 various possible pricing models. In this paper we assume a generic pricing
187 model in which the cost of a cycle from a cloud computing provider is com-

188 posed of a reservation fee and a consumption fee. Different providers' profiles
189 can be mapped onto different reservation and consumption fees. Details of
190 the pricing model are given in Subsection 3.2.

191 This paper is based on a previous work by Maciel Jr. et al. where the
192 hybrid infrastructure was presented for the first time [11]. More specifically,
193 Maciel Jr. et al. defined the hybrid IT infrastructure and its elements,
194 proposed contract planning heuristics in order to decide which contracts to
195 establish with the cloud computing provider, and evaluated the efficiency of
196 these heuristics for a limited class of applications. Their main conclusion was
197 that using information about the cloud computing provider's pricing model
198 and accurately estimating the amount of cycles that will be reclaimed from
199 the best-effort P2P grid are crucial to establishing contracts that produce a
200 high profit from running applications on the hybrid infrastructure. In this
201 paper we extend the work by Maciel Jr. et al. by: i) considering different
202 utility functions for the applications (Section 3); ii) refining the function that
203 represents the total profit yielded by running an application in the hybrid
204 infrastructure (Section 4); further investigating the impact on the efficiency
205 of the infrastructure of inaccurate predictions of the number of cycles that are
206 reclaimed from the P2P grid over a given time interval (Section 6); and, iv)
207 proposing and assessing the usefulness of a model for making this prediction
208 for a P2P grid that uses the incentive mechanism proposed by Andrade et
209 al. [12].

210 3. System Model

211 In this section we present the system model. First we describe the ap-
212 plication that we will consider, and give a model for the utility yielded by
213 its execution. Then we present the different components of the hybrid IT
214 infrastructure, with a focus on modelling the costs of the cycles from the
215 three different components.

216 3.1. The Application

217 For the sake of simplicity, we assume that during a time period Δ (typ-
218 ically on the order of a day), there is a single critical application to be exe-
219 cuted. We characterise this application by a tuple $\mathcal{A} = \langle w, t_r, u(t) \rangle$, where w
220 is an indication of the application's demand on the infrastructure, expressed
221 as the number of the cycles it requires for completion; t_r is the instant of
222 time, within Δ , when the application is ready for execution (for example the

223 instant of time when data required to run the application becomes available);
 224 and $u(t)$ is the application’s utility function. The function $u(t)$ specifies the
 225 total utility obtained by the owner of the hybrid IT infrastructure from the
 226 execution of the application, as a function of the time that the execution
 227 completes. Clearly $u(t)$ is only defined for $t \geq t_r$.

228 Figure 1 shows some examples of utility functions for time-constrained
 229 applications. For such applications the utility is a decreasing function of
 230 the instant of time at which the application completes its execution. Func-
 231 tion $step(t)$, for instance, represents a real time application whose utility is
 232 positive and constant as long as its execution completes before a deadline;
 233 for completion times longer than that, the utility drops to zero. Function
 234 $expo(t)$ is exponentially decreasing, and tends to zero as the completion time
 235 increases. Finally, function $decay(t)$ starts positive and decreases linearly as
 236 the completion time increases, becoming negative after the completion time
 237 passes a deadline. The negative utility may represent a penalty incurred if
 238 the application cannot be completed by an agreed deadline.

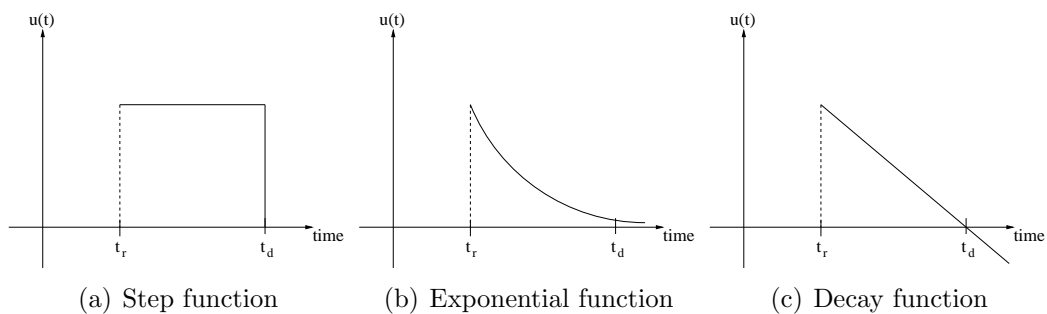


Figure 1: Some examples of utility functions

239 In this paper we consider applications with the following common pattern:
 240 there is no utility gained if the application completes its execution after a
 241 predefined deadline (t_d), i.e. $u(t) = 0, \forall t, t > t_d$. We consider three different
 242 applications. The first application, called *All-or-Nothing* (AoN), has as its
 243 sole constraint to complete its execution before the deadline. For the second
 244 application, called *Linear-Decay-until-a-Deadline* (LDuD), the utility decays
 245 linearly until it reaches the value zero at t_d . Finally, we consider an inter-
 246 mediate application, called *Graceful-Degradation-until-a-Deadline* (GDuD),
 247 whose utility decays exponentially with time. The first two applications are
 248 modelled by the following utility function:

$$249 \quad u(t) = \begin{cases} a \cdot (t - t_r) + b, & \text{if } t_r \leq t \leq t_d; \\ 0, & \text{otherwise,} \end{cases}$$

250 with $b > 0$ and $a = 0$ for the *AoN* application and $a = -b/(t_d - t_r)$ for the
 251 *LDuD* application. The third application is modelled by the following utility
 252 function:

$$253 \quad u(t) = \begin{cases} a^t + b, & \text{if } t_r \leq t \leq t_d; \\ 0, & \text{otherwise,} \end{cases}$$

254 with $b > 0$ and $a < -1$.

255 3.2. The Hybrid IT Infrastructure

256 We consider a hybrid IT infrastructure which, during the period of time
 257 Δ , is able to provide $\mathcal{C}(\Delta)$ cycles, where

$$\mathcal{C}(\Delta) = \int_{\Delta} (i(t) + g(t) + p(t)) \cdot dt,$$

258 and $i(t)$, $g(t)$ and $p(t)$ are, respectively, the number of cycles available at
 259 time t from the in-house dedicated machines, the P2P grid and the cloud
 260 computing provider.

261 We will assume that all the cycles obtained from the cloud computing
 262 market are obtained from a single provider, but our analysis can be gener-
 263 alised for the case of several providers in a straightforward way.

264 The total cost of running the hybrid infrastructure during Δ is the sum of
 265 the cost of maintaining the in-house infrastructure, the cost of donating and
 266 receiving cycles to/from the best-effort P2P grid, and the costs arising from
 267 the use of cycles from the cloud computing provider's infrastructure. We
 268 assume that the cost of maintaining the in-house infrastructure is described
 269 by a fixed cost v_i for each cycle available from the in-house infrastructure,
 270 whether or not it is used. The cost of maintaining the dedicated infrastruc-
 271 ture during Δ is therefore

$$\gamma_i(\Delta) = v_i \cdot \int_{\Delta} i(t) dt \quad (1)$$

272 We assume that the P2P grid works in an opportunistic way, with the
 273 peers only donating spare capacity to the grid which would otherwise be
 274 unused. Naturally, there is a cost v_g of donating a cycle to the grid; this
 275 is due mainly to the extra consumption of energy and to any extra security

276 enforcements that are required before tasks can be executed on behalf of other
277 peers using the spare capacity of the donating peer’s local infrastructure.
278 Nevertheless, these costs are likely to be very small compared to the other
279 costs of operating and maintaining the local infrastructure (e.g. hardware,
280 software, hosting, system administration, etc.). We therefore assume that
281 $v_g \ll v_i$, and in the rest of the paper we ignore the cost of donating idle
282 cycles to the grid. Moreover, there is no cost incurred for the cycles that are
283 claimed from the grid, since they are donated cycles.

284 The costs of the cycles obtained from the cloud computing provider de-
285 pend on the cloud computing provider’s pricing model. At the time of writ-
286 ing, very few cloud computing providers offer a fully automated negotiation
287 procedure. Most use a simple pricing model in which virtual machines are
288 brought up and torn down at the wish of the customer, who pays a fixed
289 price for each hour or fraction of hour effectively used. No reservation is
290 needed, however there is only a limited number of virtual machines that can
291 be simultaneously instantiated by a single customer. If a customer requires
292 a larger number of virtual machines, she must have previously engaged in a
293 human-to-human negotiation with the provider [33].

294 However, some cloud computing providers, such as Amazon, are starting
295 to provide a pricing model that incorporates the notion of long-term reserva-
296 tion of resources prior to their use. In this case, a lower fee is charged for the
297 use of resources if the customer has previously reserved them [34]. The cloud
298 computing market is evolving rapidly, and we believe that it cannot be as-
299 sumed that the pricing models currently used will be standard in the future.
300 In fact, Amazon’s introduction of reservation is an indication that, as more
301 and more customers enter the market, providers will look for more informa-
302 tion about customers’ likely workloads in order to be able to operate their
303 infrastructure efficiently. We predict that reservation will eventually become
304 a common feature of cloud service pricing models, and that customers will
305 be interested in software that provides some automation of the reservation
306 and contract negotiation processes. We also believe that competition among
307 providers will drive the providers to give customers more flexibility in their
308 choice of contracts.

309 Based on these predictions, we define a pricing model that we believe is
310 most likely to be adopted in the scenario that we consider in this paper, in
311 which the customer’s contract planning agent sets up short-term contracts.
312 The pricing model involves two types of fees: a reservation fee and a con-
313 sumption fee. It is reasonable to think that the urgency of a contract is a

314 critical factor in setting the reservation fee: in general, contracts which are
 315 established only shortly before the computer power is due to be consumed
 316 will tend to have more expensive reservation fees per cycle than contracts
 317 which are established well in advance. For a fixed reservation and consump-
 318 tion time, we assume that the reservation cost is directly proportional to the
 319 number of cycles that are reserved. The maximum number of cycles that
 320 can be consumed at time t is the number that has been reserved for time
 321 t at times up to and including t , however it may be that not all of these
 322 will be consumed. The reservation fee is charged for all the cycles that are
 323 reserved, whether or not they are consumed, but the consumption fee is only
 324 charged for cycles that are consumed. We assume that the consumption fee
 325 associated with a contract is directly proportional to the number of cycles
 326 consumed under the contract. Note that this pricing model is similar to the
 327 one that Amazon has started to use; however, contracts are for much shorter
 328 periods than Amazon's contracts and are negotiated automatically.

329 We represent a contract between the client and the cloud computing
 330 provider by a tuple $\mathcal{K} = \langle t_e^{\mathcal{K}}, t_u^{\mathcal{K}}, c_r^{\mathcal{K}}, \beta^{\mathcal{K}} \rangle$, where $t_e^{\mathcal{K}}$ is the time at which the
 331 contract is established; $t_u^{\mathcal{K}}$ is the time at which the cycles are to be used;
 332 $c_r^{\mathcal{K}}$ is the number of cycles reserved; and $\beta^{\mathcal{K}}$ is a number between 0 and 1
 333 expressing a relationship between the reservation and consumption fees per
 334 cycle, which is used to calculate the cost of cycles in a way detailed below.
 335 Since it does not make sense for the customer to reserve cycles for use outside
 336 the time interval $[t_r, t_d]$, we will assume that $t_u^{\mathcal{K}}$ lies in this time interval for
 337 all established contracts \mathcal{K} . When a contract is established, the cloud com-
 338 puting provider agrees to fulfil it and the customer (via the customer's agent)
 339 agrees to pay the agreed price. We assume that all contracts in compliance
 340 with the interests of provider and customer are successfully established and
 341 duly honoured by both parties involved.

342 We use the following model for the cost of c cycles under contract \mathcal{K} , where
 343 $0 \leq c \leq c_r^{\mathcal{K}}$. We write v_p for the total cost to the consumer (comprising both
 344 a reservation fee and a consumption fee) of reserving a single cycle at time t_p
 345 and consuming it at time t_d , where t_p is the earliest time at which a contract
 346 can be made for cycles to run the application, and t_d is the deadline for the
 347 execution of the application. We assume that this cost is independent of
 348 the choice of contract under which this reservation is made. (Obviously this
 349 contract has to be $\langle t_p, t_d, 1, \beta \rangle$ for some β : what we mean by the previous
 350 sentence is that the cost v_p is independent of the value of this β .) We
 351 will use a function φ of the contract establishment time and the time of

352 consumption which is independent of the choice of contract, which reflects
353 how the reservation costs vary with these times. We assume that φ is a
354 strictly decreasing function of the difference between the consumption time
355 and the contract establishment time, so that it is larger for more urgent
356 contracts, and that it takes value 1 when this difference is as large as possible,
357 i.e., $\varphi(t_p, t_d) = 1$. The cost profiles of different providers can be modelled by
358 different choices of $\beta^{\mathcal{K}}$, v_p and φ .

359 Given this, the cost of using c cycles under a contract \mathcal{K} is given by:

$$\gamma_p^{\mathcal{K}}(c) = v_p \cdot \{\beta^{\mathcal{K}} \cdot c_r^{\mathcal{K}} \cdot \varphi(t_e^{\mathcal{K}}, t_u^{\mathcal{K}}) + (1 - \beta^{\mathcal{K}}) \cdot c\}, \quad (2)$$

360 This is the sum of the cost of reserving $c_r^{\mathcal{K}}$ cycles under the contract, and the
361 consumption cost of consuming c of these reserved cycles.

362 Note that when both the reservation cost and the consumption cost are
363 taken into account, it is not true in general that given any two contracts
364 with the same time of establishment (i) if both reserve the same number
365 of cycles, it is cheaper to use the less urgent contract, or that (ii) if both
366 reserve the cycles for consumption at the same time, and both reserve at
367 least as many cycles as are actually used at that time, it is cheaper to use
368 the contract which reserves fewer cycles. As counterexamples, suppose that
369 $t_r < t_1 < t_2 < t_d$ and set $\mathcal{K}_1 = \langle t_p, t_1, 1, 0.25 \rangle$, $\mathcal{K}_2 = \langle t_p, t_2, 1, 0.875 \rangle$, $\mathcal{K}_3 =$
370 $\langle t_p, t_2, 2, 0.25 \rangle$. Then $\gamma_p^{\mathcal{K}_2}(1)$ is greater than both $\gamma_p^{\mathcal{K}_1}(1)$ and $\gamma_p^{\mathcal{K}_3}(1)$. However,
371 given any two contracts with the same time of establishment and the same
372 value of $\beta^{\mathcal{K}}$, (i) and (ii) both hold. We allow this flexibility in our general
373 pricing model, but in the evaluation sections of this paper we will assume
374 that the service provider fixes a value β and only allows the establishment of
375 contracts \mathcal{K} for which $\beta^{\mathcal{K}} = \beta$. Thus in our evaluations (i) and (ii) hold, and
376 the customer's choice of contract amounts to a choice of the time that the
377 contract is established, the time that the reserved cycles will be consumed,
378 and the number of cycles reserved. Notice also that if $\beta^{\mathcal{K}} = \beta^{\mathcal{K}'}$, $t_e^{\mathcal{K}} = t_e^{\mathcal{K}'}$, and
379 $t_u^{\mathcal{K}} = t_u^{\mathcal{K}'}$, then for all $c \leq c_r^{\mathcal{K}}$, $c' \leq c_r^{\mathcal{K}'}$ we have $\gamma_p^{\mathcal{K}}(c) + \gamma_p^{\mathcal{K}'}(c') = \gamma_p^{\mathcal{K}''}(c + c')$,
380 where \mathcal{K}'' is the contract $\langle t_e^{\mathcal{K}}, t_u^{\mathcal{K}}, c_r^{\mathcal{K}} + c_r^{\mathcal{K}'}, \beta^{\mathcal{K}} \rangle$. It follows that when calculating
381 costs in our evaluations, we can assume without loss of generality that given
382 any pair of times t_1, t_2 , at most one contract is established at time t_1 for
383 cycles to be consumed at time t_2 .

384 We assume that the customer (that is, the manager of the hybrid infras-
385 tructure) runs a planning agent [10] that is in charge of establishing contracts
386 with the cloud computing provider. The planning agent starts to run at time

387 t_p , the earliest time at which contracts can be established. Let the plan \mathcal{P} be
 388 the outcome of a run of the planning agent for the time period $\Delta = [t_p, t_d]$ \mathcal{P}
 389 is a set that contains the contracts that have been established between the
 390 customer and the cloud computing provider. Let \mathcal{U} be the usage log for the
 391 execution of part of the application, which records the use of cycles from the
 392 cloud computing provider under plan \mathcal{P} . \mathcal{U} is a set containing the values $c_u^{\mathcal{K}}$,
 393 for all $\mathcal{K} \in \mathcal{P}$, such that $c_u^{\mathcal{K}}$ is the number of cycles that have been consumed
 394 under contract \mathcal{K} during the execution accounted by \mathcal{U} . The cost incurred
 395 from the cycles reserved by a plan \mathcal{P} and used as recorded by \mathcal{U} is given by:

$$\gamma_p(\mathcal{P}, \mathcal{U}) = \sum_{\forall \mathcal{K} \in \mathcal{P}} \gamma_p^{\mathcal{K}}(c_u^{\mathcal{K}}). \quad (3)$$

396 From now on we will use the notation t^- (resp. t^+) to refer to an instant
 397 of time that is infinitesimally earlier (resp. later) than some instant of time t .
 398 During the time interval $[t_p, t_r)$, no cycles from the grid or the cloud comput-
 399 ing provider are consumed. This is because there is no critical computation
 400 to be executed in this time interval, and therefore no need for the customer
 401 to seek resources from the grid or the cloud computing provider. During this
 402 period of time, any spare cycle from the in-house infrastructure is offered
 403 to the P2P grid. For the sake of simplicity we assume that for any t with
 404 $t_p \leq t < t_r$, all $\int_{t_p}^{t_r} i(t) \cdot dt$ cycles are idle, and are, therefore, donated to the
 405 grid.

406 We now consider the number of cycles that will be available during Δ from
 407 the three different components of the hybrid infrastructure. Let t_c be the time
 408 that the application \mathcal{A} completes its execution. Thus, the number of cycles
 409 that are available from the in-house infrastructure to run the application is
 410 given by $\int_{t_r}^{t_c} i(t) dt$.

411 On the other hand, the number of cycles that are available from the
 412 P2P grid during Δ will depend on the amount of resources that have been
 413 previously donated and the quality of service that the grid is able to deliver.
 414 The grid quality of service here is related to the probability of receiving back
 415 favors paid to other peers in the grid within a certain time horizon: the
 416 favors are donations of cycles. The more rapidly that favors are paid back,
 417 the better is the quality of service of the grid. In this paper we define the
 418 grid's quality of service to be

$$\Phi = \frac{\int_{t_r}^{t_d} g(t) dt}{\int_{t_p}^{t_r} i(t) dt}$$

419 Finally, the number of cycles that are available from the cloud computing
 420 provider at time t is defined by the contracts belonging to \mathcal{P} , and is given by

$$\sum_{\{\mathcal{K} \in \mathcal{P} | t_u^{\mathcal{K}} = t\}} c_r^{\mathcal{K}}$$

421 4. Problem Statement

422 The problem that we would like to solve is how to schedule \mathcal{A} in the hybrid
 423 infrastructure, such that the associated *profit* to the owner of the hybrid
 424 infrastructure is maximised. We define the profit of running an application \mathcal{A}
 425 in the hybrid infrastructure to be the difference between the utility obtained
 426 from running \mathcal{A} and the cost of operating the infrastructure during Δ .

427 For simplicity, we assume that the application has a workload with very
 428 fine granularity, that it is sufficiently parallel that at any instant of time t it is
 429 possible, if necessary, to simultaneously schedule work using cycles available
 430 in the in-house dedicated infrastructure, in the cloud computing provider and
 431 in the P2P grid. Starting at t_r , the scheduler uses all available cycles until the
 432 execution of the application is completed, using as many in-house cycles as
 433 possible (whose cost is incurred whether or not they are used), then as many
 434 as possible of the cycles available from the grid (whose cost is negligible)
 435 and, finally, cycles available from the cloud computing provider. Following
 436 this scheduling algorithm, under the assumption that no two contracts in \mathcal{P}
 437 specify the same consumption time $t_u^{\mathcal{K}}$, the usage log \mathcal{U} associated with the
 438 execution of \mathcal{A} in the hybrid infrastructure with the plan \mathcal{P} is such that for
 439 all $c_u^{\mathcal{K}} \in \mathcal{U}$,

$$c_u^{\mathcal{K}} = \max(0, \min(c_r^{\mathcal{K}}, w - \sum_{\{c_u^{\mathcal{K}'} \in \mathcal{U} | t_u^{\mathcal{K}'} < t_u^{\mathcal{K}}\}} c_u^{\mathcal{K}'} - \int_{t_r}^{t_u^{\mathcal{K}}} (i(t) + g(t)) dt))$$

440 Note that in the scenario that we propose, the scheduling of the ap-
 441 plication is preceded by the reservation of cycles from a cloud computing
 442 provider. This makes scheduling relatively simple, but requires a solution to

443 the problem of executing the planning, i.e., deciding when and how many
 444 cycles to reserve. Different plans will lead not only to different costs, but
 445 also to different availability of cycles for running the application and, there-
 446 fore, to different values of t_c . In turn, different values for t_c lead to different
 447 utilities. In summary, using the fact that cycles obtained from the P2P grid
 448 have negligible cost, the profit that is achieved by a plan \mathcal{P} which allows the
 449 application \mathcal{A} to be completed by time t_c (where $t_r \leq t_c \leq t_d$) is:

$$\text{Profit}(\mathcal{A}, \Delta, \mathcal{P}, \mathcal{U}) = u(t_c) - \gamma_i(\Delta) - \gamma_p(\mathcal{P}, \mathcal{U}), \quad (4)$$

450 where \mathcal{U} is the usage log that results from applying the scheduling algorithm
 451 to the hybrid infrastructure under \mathcal{P} . The aim of the planning algorithm is
 452 to find the plan \mathcal{P} that maximises $\text{Profit}(\mathcal{A}, \Delta, \mathcal{P}, \mathcal{U})$.

453 5. Planning Algorithms

454 In this section, we propose planning algorithms that can be used to max-
 455 imise the profit achieved when running an application on the hybrid infras-
 456 tructure. As such, the algorithm must first estimate the number of cycles that
 457 need to be acquired from the cloud computing provider and then establish
 458 the contract or contracts that will maximise the profit.

459 The total number of cycles needed from the cloud computing provider in
 460 order to complete the execution of the application \mathcal{A} at some instant of time
 461 t_c is given by:

$$c_e(t_c) = \max(0, w - \int_{t_r}^{t_c} (i(t) + g(t)) dt).$$

462 Given the relatively short time for which the application is in execution,
 463 it is reasonable to assume that $i(t)$, for $t_r \leq t \leq t_c$, is known at time t_p , when
 464 the planner starts to run. Unfortunately, due to the uncertainty inherent in
 465 the best-effort P2P grid, it may not be possible at time t_p to predict $g(t)$
 466 accurately for $t_r \leq t \leq t_c$.

467 Note that if it is possible at time t_p to estimate $c_e(t)$ accurately for any
 468 t in $[t_r, t_d]$, then, for the system model that we have defined in Section 3
 469 with the additional assumption that $\beta^{\mathcal{K}}$ is the same for all contracts \mathcal{K} that
 470 can be established, it is straightforward to find a plan that maximises the
 471 profit. There is a plan consisting of a single contract $\langle t_p, t_u, c_e(t_u), \beta \rangle$ for

472 which the profit is maximal. A simple solver can be used to find the time
473 t_u that specifies this contract. For instance, for the *AoN* application whose
474 utility is a positive constant for any t_u , $t_u \leq t_r \leq t_d$, (and still making the
475 assumption that only contracts \mathcal{K} with $\beta^{\mathcal{K}} = \beta$ can be established), it is easy
476 to see that the contract required is $\langle t_p, t_d, c_e(t_d), \beta \rangle$, because out of all the
477 contracts that can be established which give rise to the maximum utility,
478 this is the least urgent contract reserving the smallest number of cycles, and
479 hence has the minimum cost.

480 In the approach sketched above, underestimation of the number of cycles
481 that will be received from the grid leads to an overestimation of $c_e(t)$ and
482 the reservation of more cycles than is necessary. It may be the case that this
483 results in higher reservation costs than if only the cycles that will actually
484 be used had been reserved, and in this case the profit achieved may not be
485 maximal. (It is possible that it may still be maximal if the extra cycles from
486 the grid enable the application to finish execution earlier than expected, re-
487 sulting in a higher utility.) On the other hand, overestimation of the number
488 of cycles that will be received from the grid leads to the underestimation of
489 $c_e(t)$, and as a result, at time $t_u^{\mathcal{K}}$ there will be still some part of the applica-
490 tion workload left to be processed. There will hence be unexpected costs of
491 purchasing the additional cycles from the cloud computing provider required
492 to complete the execution of the application (if this is possible), and the
493 application will complete later than expected and so may produce a smaller
494 utility than expected. Thus the profit will be lower than was expected by the
495 planner at the time it established the relevant contracts, and it is possible
496 that a different choice of contracts would have led to a higher profit.

497 Since it is not generally possible to predict with complete accuracy the
498 number of cycles that will be available from the grid over a future time
499 interval, we resort to heuristics that try to achieve profits that are as close
500 as possible to the maximal achievable. These heuristics assume that $\beta^{\mathcal{K}} = \beta$
501 is the same for all contracts \mathcal{K} that can be established, and also that for any
502 t_e, t_u with $t_p \leq t_e < t_u$, $t_r \leq t_u \leq t_d$ and any positive integer c , it is possible
503 to establish a contract $\langle t_e, t_u, c, \beta \rangle$.

504 Out of all possible heuristics, we concentrate our focus on those that make
505 at most two contracts within the $\Delta = [t_p, t_d]$ time interval. In particular, we
506 assume that one contract (\mathcal{K}_1) is always established as soon as possible, at
507 time t_p , while the second contract (\mathcal{K}_2), when needed, is established at the
508 instant of time at which the cycles reserved in the first contract were used,
509 i.e., $t_e^{\mathcal{K}_2} = t_u^{\mathcal{K}_1}$. The reason is as follows. The heuristic runs a solver to

510 find the contract \mathcal{K}_1 that maximises the profit, given an estimate c'_g (which
511 depends on $t_u^{\mathcal{K}_1}$) of the number of cycles that are going to be received from
512 the grid in the interval $[t_r, t_u^{\mathcal{K}_1}]$. By time $t_u^{\mathcal{K}_1}$ the heuristic can evaluate how
513 accurate the estimate was. If the number of cycles that have been received
514 from the grid in this time interval (we denote this number c_g) is greater than
515 or equal to c'_g , then the execution of the application was completed at or
516 before $t_u^{\mathcal{K}_1}$, and no further action is required. On the other hand, if $c'_g < c_g$
517 an additional contract may be necessary to complete the execution of the
518 application. At this point the heuristic carries out a new optimisation, this
519 time considering only the workload left to be processed. To avoid having
520 to establish a third contract, the heuristic takes a conservative approach
521 and assumes that no further cycles will be received from the grid before the
522 execution of the application is completed.

523 In this paper we evaluate different flavours of this heuristic framework
524 that differ from each other in how they produce the estimate c'_g . We discuss
525 each of them in turn.

526 **Omniscient Heuristic.** This heuristic produces an optimal plan. We as-
527 sume in this case that the heuristic has access to an oracle that is able to
528 predict c_g with complete accuracy, i.e., we suppose that $c'_g = c_g$. This heuris-
529 tic therefore always makes a single contract for the precise amount of extra
530 cycles needed from the cloud computing provider to compute the workload.
531 Thus, this heuristic always achieves the maximum profit for the hybrid in-
532 frastructure.

533 **Averse Heuristic.** This heuristic is completely averse to the risk of trusting
534 the best-effort grid. Therefore it assumes that $c'_g = 0$. It always establishes
535 a first contract for all the cycles needed to compute the workload, i.e., for
536 the difference between w and the cycles that will be provided by the in-house
537 infrastructure over the relevant time interval. Obviously, in this case there
538 is also no need to make a second contract. Although this heuristic estimates
539 that no cycles will be received from the grid, the scheduling algorithm uses
540 the cycles that may in fact be provided by the grid, potentially reducing the
541 number of cycles consumed from the cloud computing provider.

542 **Oblivious Heuristic.** This heuristic is oblivious to the existence of the grid,
543 and therefore it also assumes that $c'_g = 0$. Moreover, when evaluating this
544 heuristic we ignore $g(t)$ and instead assume that $g(t) = 0$ within Δ : another
545 way of thinking about this is that we assume that the scheduling algorithm
546 does not use any cycles available from the grid. Once again, in this case only
547 a single contract is established. Under our assumptions on which contracts

548 can be established and on the pricing model, this heuristic makes the optimal
 549 choice of contracts for a hybrid infrastructure that does not have access to
 550 a P2P grid. Thus, when we compare the other heuristics with this one, we
 551 can measure the value that the P2P grid adds to the hybrid infrastructure.

552 **Predictive heuristic.** This heuristic uses an oracle to obtain some knowl-
 553 edge about the grid’s behaviour, as the *Omniscient* does, however the ora-
 554 cle used by the predictive heuristic is imperfect. We model this imperfec-
 555 tion by associating a nonzero error ξ with the prediction that it makes, i.e.
 556 $c'_g = c_g \cdot (1 \pm \xi)$. Since this heuristic may need to establish a second contract
 557 to complete the execution of the application, the instant of time to use the
 558 cycles of the first contract has to be smaller than t_a , otherwise it would not
 559 always be possible to establish a second contract (recall that $t_e^K < t_u^K$).

560 In summary, the *Omniscient* and *Oblivious* heuristics produce bench-
 561 marks for the profit that can be achieved by the execution of the application
 562 on the hybrid infrastructure. The *Averse* heuristic reveals the value that
 563 the grid adds to the infrastructure. Finally, the *Predictive* heuristic allows
 564 us to evaluate the impact that the quality of the estimation of the amount
 565 of resources received from the grid has on the profit that can be achieved.
 566 Algorithm 1 is the pseudo-code for the planner framework just described.

567 6. Evaluation of the Heuristics

568 6.1. Evaluation Metric

569 To measure the efficiency of a given heuristic, we compare the profit
 570 yielded by this heuristic with that yielded by the Omniscient and the Obliv-
 571 ious heuristics. We define the *efficiency* achieved by a heuristic H when
 572 running an application \mathcal{A} on the hybrid infrastructure as follows:

$$\mathcal{E}_H = 1 - \frac{Profit_{Omniscient}(\mathcal{A}) - Profit_H(\mathcal{A})}{Profit_{Omniscient}(\mathcal{A}) - Profit_{Oblivious}(\mathcal{A})},$$

573 where $Profit_{Omniscient}(\mathcal{A})$, $Profit_{Oblivious}(\mathcal{A})$ and $Profit_H(\mathcal{A})$ are, respec-
 574 tively, the profit achieved by the Omniscient heuristic, Oblivious heuristic
 575 and H , when scheduling A over the same hybrid infrastructure and under
 576 the same conditions.

577 Notice that the efficiency is not defined if the profit of the Omniscient
 578 heuristic is equal to that of the Oblivious heuristic. Note also that 1 is
 579 an upper bound for the efficiency, but there is no lower bound for it: the
 580 efficiency may be negative. This would be the case if the choice of contracts

Algorithm 1: Planner's algorithm

```
begin
  at time =  $t_p$  do
    begin
      estimate  $c'_g$  according to Heuristic
      find  $t_u^{\mathcal{K}_1}$  such that Equation 4 is maximised with
         $\mathcal{P} = \{\mathcal{K}_1\}$ ,  $t_e^{\mathcal{K}_1} = t_p$  and  $c_r^{\mathcal{K}_1} = w - c'_g - \int_{t_r}^{t_u^{\mathcal{K}_1}} i(t)dt$ 
      establish contract  $\mathcal{K}_1$ 
    end
    at time =  $t_u^{\mathcal{K}_1}$  do
      begin
        let  $w'$  be the number of cycles that still need to be processed
        if ( $w' > 0$ )
          begin
            find  $t_u^{\mathcal{K}_2}$  such that Equation 4 is maximised with
               $\mathcal{P} = \{\mathcal{K}_2\}$ ,  $t_e^{\mathcal{K}_2} = t_u^{\mathcal{K}_1}$  and  $c_r^{\mathcal{K}_2} = w' - \int_{t_u^{\mathcal{K}_1}}^{t_u^{\mathcal{K}_2}} i(t)dt$ 
            establish contract  $\mathcal{K}_2$ 
          end
        end
      end
    end
  end
```

581 made by the heuristic was so bad that the resulting profit was even lower
582 than that attained by the Oblivious heuristic.

583 6.2. Description of the Scenarios Evaluated

584 To evaluate the heuristics using the model presented in Section 3 we
585 need to define scenarios by setting values for the constants and instantiating
586 the functions that comprise the model. We first discuss the constants and
587 functions related to the application, and then we discuss those related to the
588 infrastructure.

589 Regarding the application, we need to define its workload (w), its utility
590 function and its lifetime (t_r and t_d). Based on the experience of the e-
591 Science applications currently used by the OurGrid Community, we set the
592 workload to be that of an application running in a twenty-machine cluster
593 for approximately 12 hours. Thus, we have $w = 864,000$ cycles and $t_d - t_r =$
594 $43,200$ seconds (12 hours). We set $t_p = 0$ and assume that Δ is a time interval

595 of 24 hours. Therefore, $t_r = 43,200$ seconds and $t_d = 86,400$ seconds. For
 596 the utility function of the *AoN* and *LDuD* applications, the value b gives the
 597 *maximum* revenue that can be achieved with the execution of the application:
 598 if the execution of the application finishes exactly at t_r , the revenue obtained
 599 is b units of utility. We assume that the utility obtained by the completion of
 600 the application is directly proportional to its processing demand. Therefore,
 601 we set b to be $\mu \cdot w$ (with $\mu > 1$), where μ is the maximum profitability
 602 factor of the application. For example, $\mu = 2$ means that 2 units of utility
 603 is obtained as a result of the execution of the application for each unit of
 604 workload that the application contains. For the *GDuD* application we set
 605 $a = -1.00017$ and $b = 1.00054 \cdot \mu \cdot w$, which provides a utility that decreases
 606 slowly until about 8 hours after t_r , and has a sharp decrease after that.

607 We assume that the cost of the in-house infrastructure over a time interval
 608 is equal to the number of cycles that are available from the in-house machines
 609 over that interval, i.e. we set $v_i = 1$. We set v_p , the cost of reserving a cycle
 610 from the cloud service provider at time t_p and consuming it at time t_d , as a
 611 function of v_i . In the scenarios we evaluated we set $v_p = 0.5 \cdot v_i$, assuming
 612 that the cloud provider is able to operate its infrastructure more than twice
 613 more efficiently than the in-house infrastructure is operated.

614 As indicated earlier, we assume that the cloud service provider sets a
 615 value β and only allows contracts \mathcal{K} to be established for which $\beta^{\mathcal{K}} = \beta$.
 616 In order to evaluate different providers' profiles, we consider three different
 617 values for β : $1/2$, $2/3$, and $3/4$.

618 The function φ , which reflects how the reservation fees vary with different
 619 contract establishment times and consumption times, is set as follows. We
 620 set $\varphi(t_1, t_2)$ to be a hyperbolically decaying function of $t_2 - t_1$ given by:

$$\varphi(t_1, t_2) = \frac{18,000}{t_2 - t_1 + 5,600} + 0.8,$$

621 which leads to a value for the contracts to be approximately 4 for the most
 622 urgent ones ($\varphi(t, t^+)$) and approximately 2, 5 for the contracts established at
 623 least 12 hours in advance. This allows us to investigate the behaviour of the
 624 heuristics in scenarios in which the cost of the contracts change substantially.

625 We specify three grid profiles by their quality of service Φ : a *bad* quality
 626 grid with $\Phi = 0.1$, a *medium* quality grid with $\Phi = 0.5$, and a *good* quality
 627 grid with $\Phi = 0.9$. For instance, for the good quality grid, the number of the
 628 cycles that are available from the grid during $[t_r, t_d]$ is 90% of the number

629 donated to the grid during $[t_p, t_r^-]$ ($\int_{t_r}^{t_d} g(t) \cdot dt = 0.9 \cdot \int_{t_p}^{t_r^-} i(t) \cdot dt$). However,
630 it is reasonable to suppose that the number of cycles available from the grid
631 during a subinterval of $[t_r, t_d]$ is smaller for an earlier subinterval than for
632 a later subinterval of the same length, because when the later time interval
633 starts a smaller number of outstanding favors (donated resources) need to be
634 paid back from the grid to the peer representing the in-house infrastructure.
635 We therefore set $g(t)$ to be the following decreasing function of t :

$$g(t) = 2 \cdot \Phi \cdot (t_d - t_r)^{-2} \cdot (t_d - t) \cdot \int_{t_p}^{t_r^-} i(t') dt'.$$

636 6.3. Numerical Results

637 For simplicity, we assume that the capacity of the in-house infrastructure
638 does not change during the time interval Δ , and we introduce the *capacity*
639 *ratio* λ ($0 < \lambda < 1$) which expresses how much of the workload w can be
640 processed in-house. For instance, $\lambda = 0.5$ means that the in-house capacity
641 can compute 50% of the application's workload. Note that when $\lambda = 0$
642 there are no in-house resources available during Δ , and when $\lambda = 1$ all the
643 workload can be processed in-house. Neither of these scenarios are of interest
644 to our study. The figures for this subsection show graphs of the efficiency
645 versus the capacity ratio λ for $\lambda \in \{0.1, 0.2, \dots, 0.9\}$. We will first describe
646 the general results for all scenarios evaluated, and then discuss the impact
647 of particular parameters on the efficiency obtained by the heuristics.

648 In general, t_c is calculated as a compromise between the loss of utility as
649 t_c increases and the reduction in cost by avoiding to contract at the cloud
650 provider the cycles that are obtained from the in-house infrastructure and the
651 P2P grid during the time interval $[t_r, t_c]$. However, for the *LDuD* application,
652 in all scenarios evaluated, all heuristics took the decision to contract all extra
653 cycles to be used exactly at t_r . This is because for the *LDuD* application,
654 as t_c increases, the loss in utility is more important than the cost reduction
655 associated. Thus, in all scenarios the profit yielded by both the Omniscient
656 and the Oblivious heuristics were the same and the efficiencies for the other
657 heuristics were not defined. Therefore, in the following we discuss only the
658 efficiency values for the *AoN* and the *GDuD* applications.

659 Figure 2 shows the average efficiency obtained by the heuristics on all the
660 scenarios evaluated, Figure 2(a) for the *AoN* application, and Figure 2(b)
661 for the *GDuD* application. These figures show the efficiency of the *Averse*

662 heuristic, and of the *Predictive* heuristic for the cases where the heuristic's
 663 estimate of the number of cycles available from the peer-to-peer grid is 10%
 664 smaller, 10% greater, 30% smaller or 30% greater than the true number.

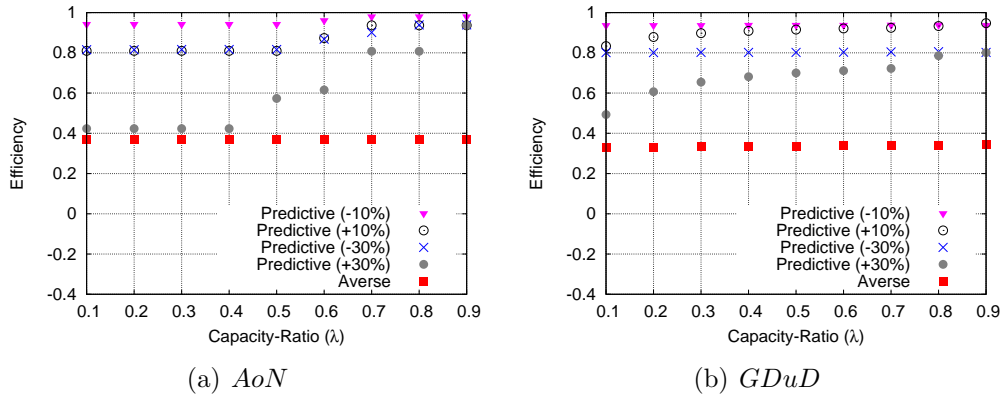


Figure 2: Average efficiency versus capacity ratio (λ).

665 As expected, for the relatively low errors in the estimation of the cycles
 666 received from the grid, the *Predictive* heuristic provides better results than
 667 the *Averse* heuristic, since it makes use of its partial knowledge of the grid's
 668 behaviour. When the *Predictive* heuristic underestimates the number of cycles
 669 available from the grid, the results are better than when it overestimates
 670 this number. This is because when it overestimates the number of cycles
 671 available from the grid it reserves fewer cycles from the cloud computing
 672 provider in its first contract than are necessary to complete the application,
 673 and has to establish a second contract later on. This results in higher reser-
 674 vation fees than if all the cycles necessary to complete the application had
 675 been reserved in the first contract.

676 For the *AoN* application (see Figure 2(a)), the *Predictive* heuristic has
 677 higher efficiency for larger values of λ , because the larger the in-house capac-
 678 ity is the more idle cycles it donates to the grid, and thus the more cycles
 679 the grid is likely to pay back within the time interval $[t_r, t_c]$. For the *GDuD*
 680 application (see Figure 2(b)) λ has less impact on the efficiency of the *Predic-*
 681 *tive* heuristic, because the completion time for the execution of the algorithm
 682 is generally earlier than t_d , and so the heuristic does not take advantage of
 683 all the in-house and grid capacity available before the deadline t_d .

684 The *Averse* heuristic ignores the grid and reserves all the cycles it needs
 685 (and which will not be provided in-house) from the cloud computing provider.

686 This results in a very low efficiency for all the scenarios we investigate. This
687 efficiency is not affected by the value of λ . When λ increases, the number
688 of cycles likely to be available from the grid increases, reducing the probable
689 cost of running the application. However, this cost reduction is also achieved
690 by the other heuristics. By taking a closer look at our results, we discovered
691 that when λ increases the profits obtained by the *Omniscient*, *Oblivious* and
692 *Averse* heuristics increase by the same proportion, leaving the efficiency for
693 the *Averse* heuristic unchanged.

694 We evaluated the impact on efficiency of the quality of service Φ of the
695 grid, setting $\Phi \in \{0.1; 0.5; 0.9\}$. Figure 3 presents the average efficiency
696 obtained for each value of Φ , for both The *AoN* and the *GDuD* applications.
697 Not surprisingly, the efficiency of the *Averse* heuristic is unaffected by Φ . On
698 the other hand, the *Predictive* heuristic performs better as the grid’s quality
699 of service improves, and achieves efficiency 1 for some of the scenarios in
700 which Φ and λ are large.

701 Figure 4 presents the average efficiency obtained for different values of
702 β . It can be seen from this figure that as β increases the efficiency of the
703 heuristics decreases, and that β has a greater effect on the *Averse* heuristic,
704 which reserves more cycles from the cloud computing provider than the other
705 heuristics do.

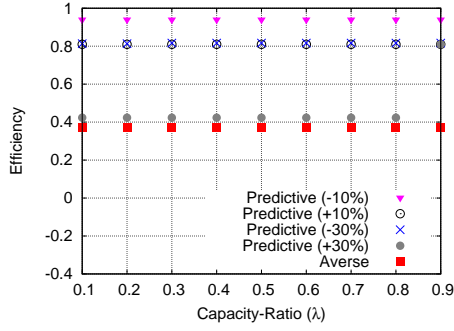
706 In summary, our results show that it is important to use at least knowl-
707 edge about the grid behaviour when deciding which contracts to establish
708 with the cloud computing provider. So, constructing an estimation for the
709 behaviour of the grid is essential for making contracts that lead to high effi-
710 ciency in the use of the hybrid infrastructure.

711 7. Estimating the Quality of Service of a P2P Grid

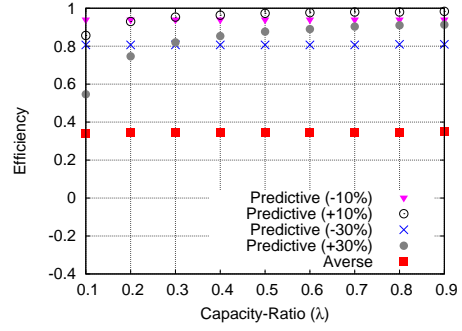
712 In this section we propose and evaluate an analytical model that can be
713 used to estimate, at a given instant of time, the amount of resources that
714 will be reclaimed from a best-effort P2P grid in the near future.

715 7.1. Model of the P2P Grid

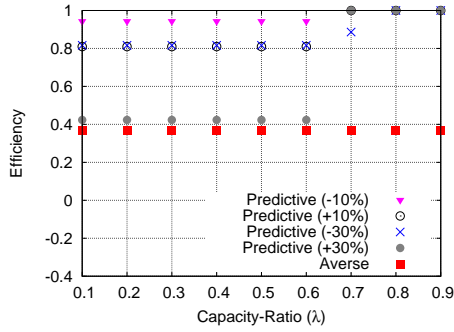
716 Our model is of a P2P grid that operates an incentive mechanism called
717 the “Network of Favors” [12] which is used in the OurGrid middleware [1].
718 This incentive mechanism uses information that each peer gathers about its
719 past interactions with other peers in the grid. For each peer p' with which
720 it interacts, peer p records a *balance* that represents the difference between



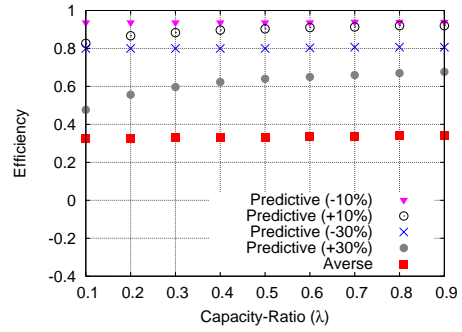
(a) $\Phi = 0.1, AoN$



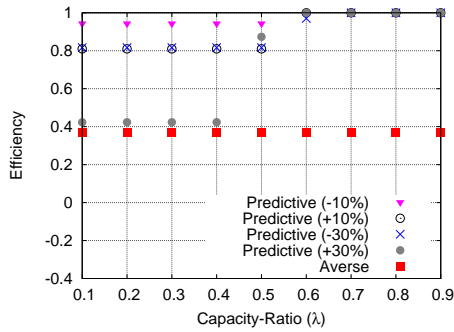
(b) $\Phi = 0.1, GDuD$



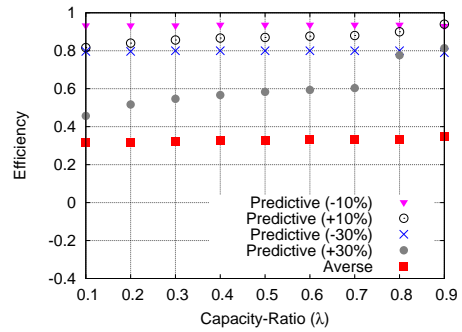
(c) $\Phi = 0.5, AoN$



(d) $\Phi = 0.5, GDuD$

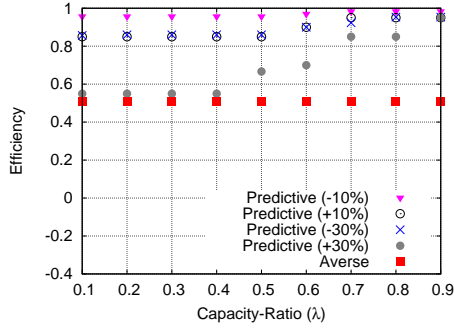


(e) $\Phi = 0.9, AoN$

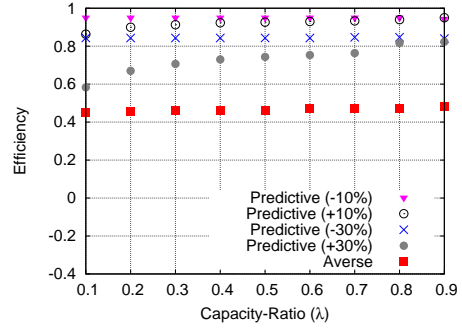


(f) $\Phi = 0.9, GDuD$

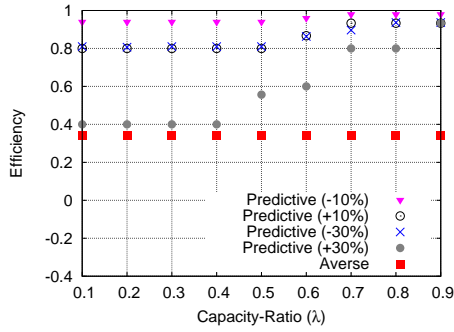
Figure 3: Efficiency versus capacity ratio (λ) for grids with different quality of service (Φ).



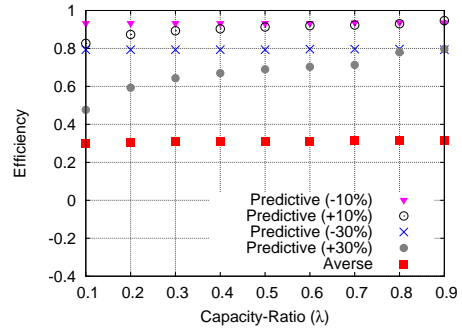
(a) $\beta = 1/2, AoN$



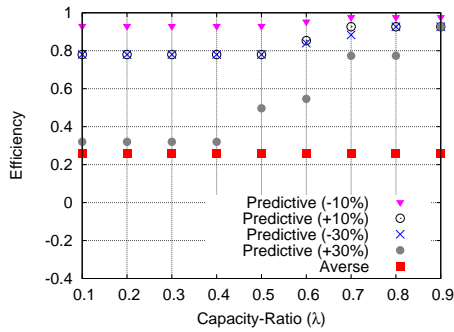
(b) $\beta = 1/2, GDuD$



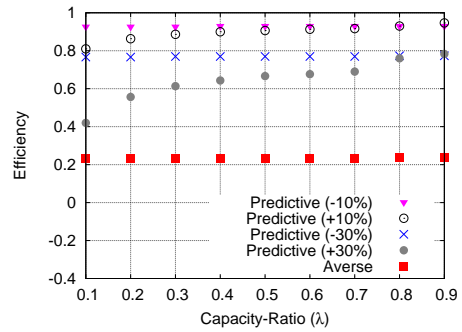
(c) $\beta = 2/3, AoN$



(d) $\beta = 2/3, GDuD$



(e) $\beta = 3/4, AoN$



(f) $\beta = 3/4, GDuD$

Figure 4: Efficiency versus capacity ratio (λ) for different values of β .

721 the number of resources that it has received from p' and the number of
722 resources that it has donated to p' . This balance is zero if p and p' have
723 never interacted. It increases when p donates resources to p' and decreases
724 when p consumes resources from p' , unless it is already zero: as a defence
725 against whitewash attacks, the balance never takes negative values. Peer p
726 allocates its idle resources proportionally according to the balances of the
727 peers that request these resources. If all these peers have zero balances, p
728 distributes its idle resources equally among them. This simple approach has
729 been shown to be efficient at discouraging free riding.

730 The model we propose of the P2P grid is designed to be used by a peer
731 p_0 (which we will call the “local peer”) that wants to estimate the number
732 of resources it will obtain from the grid during a given period of time in
733 the near future, during all of which time it will request resources from the
734 grid. In the eyes of the local peer, the grid is composed by a set of remote
735 peers $G = \{p_1, p_2, \dots, p_N\}$, where N is the number of peers in the grid
736 other than p_0 . Each peer can be either in *consuming* state - when it is
737 requesting resources from the grid - or in *donating* state - when it has idle
738 resources available for use by other peers in the grid. A peer will never be in
739 both states at the same time, as we assume that peers only ask for remote
740 resources if there are not enough local resources available. We write $G_c(t)$ for
741 the set of peers in G that are in consuming state at time t . We assume that
742 there is high contention for the grid’s resources; specifically, we assume that
743 every resource a donating peer makes available to the grid is consumed by
744 some peer, and that if there are any peers in consuming state with positive
745 balance then all the resources that the donating peer makes available will be
746 consumed by these peers, with none left over for peers with zero balance.

747 Assuming that $b_k^i(t)$ is the balance peer p_i associates with peer p_k at time
748 t , we can introduce the aggregate balance of all consuming peers other than
749 the local peer p_0 on the provider peer p_i at time t , given by

$$B_i(t) = \sum_{\forall p_k \in G_c(t)} b_k^i(t)$$

750 Therefore, as a result of the Network of Favors mechanism, a donating
751 peer p_i provides part of the $r_i(t)$ resources available on its infrastructure at
752 time t to the consuming peer p_0 according to the following equation.

$$R_0^i(t) = \begin{cases} \frac{b_0^i(t)}{B_i(t)+b_0^i(t)} \cdot r_i(t) & \text{if } B_i(t) + b_0^i(t) > 0 \\ \frac{r_i(t)}{|G_c(t)|+1} & \text{otherwise} \end{cases}$$

753 When resources are consumed, the balances from both consumer and
754 provider are updated. For the sake of simplicity, we assume that all peers
755 use the same accounting function, and that each donated resource results in
756 an addition or subtraction of one unit from the relevant balances (with the
757 exception that when a balance is zero no units are subtracted from it). Thus,
758 the changes at time t in the balances b_0^i and b_i^0 for the consuming peer p_0
759 and a donating peer p_i are given by

$$\frac{b_0^i(t)}{dt} = -\min(R_0^i(t), b_0^i(t)) \quad (5)$$

and

$$\frac{b_i^0(t)}{dt} = R_0^i(t)$$

760 The total amount of resources obtained from the grid by the local peer
761 p_0 from all peers at time t is:

$$R_0(t) = \sum_{\forall p_i \in G \setminus G_c(t)} R_0^i(t) \quad (6)$$

762 However, in practice the local peer will not be able to apply Equation 6
763 to determine the number of resources that it will obtain from the grid, as
764 the values of many parameters are difficult or even impossible for this peer
765 to know. For instance, the aggregate balance $B_i(t)$ is a piece of information
766 that is stored only at p_i . Instead of using Equation 6, we propose a prediction
767 model that uses more generic parameters which can be estimated more easily.
768 The prediction model takes into account the possible presence of A peers with
769 altruistic behaviour (they are hardly ever in consuming state). The balances
770 that altruistic peers record will be zero most of the time, as altruistic peers
771 rarely (if ever) ask favors to the grid. Thus, altruistic peers will usually
772 distribute their idle resources equally among all consuming peers, no matter
773 whether one of the consuming peers donated more than others in the past.

774 For our model, we suppose that at any time t each peer has an indepen-
775 dent probability ρ of being in donating state, and that the resources that a
776 donating peer provides at time t is distributed independently of t and of the

777 consuming peer's identity, and has mean \bar{r} . If the local peer p_0 is in con-
 778 sumption state at time t , it follows that the expected number of resources
 779 available from all the donating peers at this time is $\bar{r} \cdot N \cdot \rho$.

780 We estimate the number of resources obtained from the grid by the local
 781 peer p_0 at time t by:

$$E(t) = \begin{cases} \bar{r} \cdot (N \cdot \rho - A) \cdot \frac{\bar{b}_0(t)}{\bar{B}(t) + \bar{b}_0(t)} + \frac{A \cdot \bar{r}_A}{N \cdot (1 - \rho) + 1} & \text{if } \bar{B}(t) + \bar{b}_0(t) > 0 \\ \bar{r} \cdot N \cdot \rho \cdot \frac{1}{N \cdot (1 - \rho) + 1} & \text{otherwise} \end{cases} \quad (7)$$

782 where $\bar{b}_0(t)$ is the estimated aggregate balance of the local peer p_0 on all
 783 donating peers at time t ; $\bar{B}(t)$ is the estimated aggregate balance of all
 784 consuming peers other than the local peer on all donating peers at time
 785 t ; and \bar{r}_A is the mean number of resources available from altruistic peers at
 786 time t .

787 Nevertheless, the local peer wants to be able to estimate not only the
 788 amount of resources it will obtain at time t , but more importantly the esti-
 789 mated amount of resources to be obtained in a time period $[t_s, t_f]$ in the near
 790 future, given by:

$$\Psi([t_s, t_f]) = \int_{t_s}^{t_f} E(t) dt \quad (8)$$

791 When applying Equation 8, we have to consider the change rate over time
 792 for $\bar{B}(t)$ and $\bar{b}_0(t)$. We make the simplifying assumption for our model that
 793 $\bar{B}(t)$ is constant over the time we are predicting. This assumption is based
 794 on the fact that, while consuming peers have their balances decreased by
 795 consuming resources, the providing peers have their balances increased by
 796 donating them. Thus, if peers frequently change their state from donating to
 797 consuming and vice-versa during the time period for which we are predicting,
 798 the aggregate balance of all peers will not change much over this short period
 799 of time, and we can use its mean value over this time period as an estimate
 800 of its value at any particular time during that period.

801 As mentioned before, the balance b_0^i will not increase, and may decrease,
 802 over a time interval during which the local peer p_0 is in consuming state.
 803 When this balance decreases, it affects the number of resources that the
 804 local peer can expect to be obtained from p_i . Thus, we need to model the
 805 dynamics of these balances. Since we do not know the value $R_0^i(t)$ we cannot

806 use Equation 5 directly. However, we can estimate $R_0^i(t)$ by $E(t)$, using
 807 Equation 7, and use its result to estimate the decay rate of the aggregate
 808 balance $\bar{b}_0(t)$ while p_0 is in consuming state. We assume that no decrease to
 809 the aggregate balance $\bar{b}_0(t)$ will result from the donation of resources to p_0
 810 by altruistic peers, because if p_i is an altruistic peer then b_i0 is very likely to
 811 be zero before (and after) the donation. Our estimate of the change rate of
 812 $\bar{b}_0(t)$ is therefore:

$$\frac{\bar{b}_0(t)}{dt} = -\min\left(E(t) - \frac{A \cdot \bar{r}_A}{N \cdot (1 - \rho) + 1}, \bar{b}_0(t)\right) \quad (9)$$

813 We can now use estimates of the aggregate balances $\bar{b}_0(t_s)$, $\bar{B}(t_s)$ at the
 814 initial time t_s , along with Equation 7 and the differential Equation 9, to
 815 calculate $E(t)$; and then apply Equation 8 to obtain an estimate of the total
 816 amount of resources that will be received by p_0 from the grid during the time
 817 period $[t_s, t_f]$, as required.

818 7.2. Evaluation of the grid model

819 We evaluate the grid model by comparing the prediction that it gives
 820 for the amount of resources that the local peer will receive with simulation
 821 results using field data. For our simulations we have used traces obtained
 822 from the execution of real grids, provided by the Grid Workloads Archive
 823 (GWA) [13, 35], an initiative of University of Delft for centralising access to
 824 workload traces from grid environments. Among the traces that GWA pro-
 825 vides, we have chosen the ones from NorduGrid, which is a grid for academic
 826 researchers in nordic countries that has been operating since 2002 [36]. We
 827 have chosen this trace because, for the purposes of our simulations, it is the
 828 most suitable of all traces available: it has the highest number of sites (75
 829 sites) with resource contention scenarios (781,370 tasks run), lasts for a long
 830 time (about 3 years) with most of the applications being bag-of-tasks.

831 As we wanted to simulate scenarios with a number of peers higher than
 832 the number of sites available on the trace, we divided the trace into time
 833 windows of 2 months and randomly selected sites from each time window,
 834 assigning a different peer to each site, until we had the desired number of
 835 peers. We then grouped together all the behaviours of the selected sites to
 836 make the workload. The number of peers (N) is a parameter of the simulator.
 837 We use a normal distribution to set the amount of resources for each peer,
 838 based on the work by Kee et al. [37], which models the number of nodes

839 per cluster on computational grids. The mean amount of resources per peer
840 (\bar{r}) used on the normal distribution is an input of the simulator, and the
841 standard deviation value is set such that 99.7% of the distribution values are
842 between $0.5\bar{r}$ and $1.5\bar{r}$. The workload was built based on the following job
843 information available: submit time, run time, number of requested processors
844 and job origin site for each task recorded in the trace. The workload was
845 filtered in order to use only tasks that requested a single processor, since
846 we are simulating a desktop grid infrastructure that only supports bag-of-
847 tasks submissions. This filtering removed less than 1% of the trace from
848 the simulation workload. For the sake of simplicity, we also considered that
849 machines in the grid were homogeneous and each contained a single processor.

850 The prediction model given in Subsection 7.1 estimates the amount of
851 resources that the local peer will be obtain from the grid in a specified time
852 interval. However, a peer with low resource requirements (or with high re-
853 source requirements which are however almost all met by its in-house in-
854 frastructure) may consume fewer resources than are available to it from the
855 grid. Since the prediction model does not consider the amount of resources
856 requested from the grid by the local peer, we have to consider this issue in
857 our evaluation. In order to do that, we evaluated the model by comparing the
858 ratio between the estimated and requested amount of resources (ER) with
859 the ratio between the obtained and requested amount of resources (OR).
860 We set an upper bound of 100% for ER , meaning that if the amount of re-
861 sources that the model estimated was higher than the amount of resources
862 requested then we reset ER to 100%, as no more than the amount of re-
863 sources requested can actually be used. Formally, given a simulation S and
864 an estimate $estimated(S)$ of the amount of resources that will be available
865 from the grid during the time period simulated by S , where the estimate is
866 obtained by using the prediction model, the values of ER and OR for this
867 simulation are given by:

$$ER = \min \left(\frac{estimated(S)}{requested(S)}, 1 \right)$$

$$OR = \frac{obtained(S)}{requested(S)}$$

868 where $requested(S)$ and $obtained(S)$ are the amounts of resources that were
869 requested and obtained over the course of the the simulation.

870 To evaluate the model for this simulation, we calculate an error which is
 871 defined as the difference between the ratio ER given by the model and the
 872 ratio OR given by the simulations:

$$\xi = ER - OR \quad (10)$$

873 If in some scenario the amount of resources available from the grid is
 874 larger than the amount that the peer requests, it is likely that for this scenario
 875 the error will be zero, because provided that the estimate of the amount of
 876 resources that will be available is at least as large as the amount requested,
 877 both ER and OR will take value 1. Since our prediction model assumes
 878 that there is high contention in the grid, we evaluate only the parts of the
 879 trace for which the amount of obtained resources is smaller than the amount
 880 requested, i.e., when the demand for resources outstrips the supply. When
 881 supply exceeds demand, all resource requests will be satisfied.

882 We simulated each scenario several times using each peer in turn as the
 883 local peer, setting different values for the number of peers N (the values
 884 used for N were 100 and 200) and for \bar{r} (the values used for \bar{r} were 10,
 885 20, and 40). We divided the resulting 2-month-long simulations into shorter
 886 simulations with lengths of 1, 2, ... 50 hours. For each of these shorter
 887 simulations, we used the grid model to predict the amount of resources which
 888 would be available from the grid during the time period of the simulation,
 889 and calculated the prediction error ξ for this simulation. Fixing $N = 200$
 890 and varying values for \bar{r} , then fixing \bar{r} and varying values for N , and for each
 891 $\Delta t \in \{1, 2, \dots, 50\}$ we calculated the mean value of ξ for the set of simulations
 892 whose length was Δt hours. Then we calculated the mean $\bar{\xi}$ of these 50 mean
 893 values.

894 Table 1 summarises the results. The first column gives the number of
 895 peers N in the grid. The second column gives the mean amount of resources
 896 offered by a donating peer (\bar{r}). The third column is the mean of the mean
 897 overestimated prediction errors (positive errors) over all the shorter simula-
 898 tion lengths ($\bar{\xi}_+$). The fourth column is the mean of the mean underestimated
 899 prediction errors (negative errors) over all the shorter simulation lengths
 900 ($\bar{\xi}_-$). The last column gives the frequency of positive errors, i.e., the number
 901 of simulations for which the model overestimated the amount of resources
 902 received from the grid, divided by the total number of simulations.

903 Out of the pairs of values for N and \bar{r} for which we have run simulations,
 904 the one that gives rise the highest value of overestimated $\bar{\xi}_+$ is $N = 200$, $\bar{r} =$

| N | \bar{r} | $\bar{\xi}_+$ | $\bar{\xi}_-$ | %Overestimated |
|-----|-----------|---------------|---------------|-----------------------|
| 100 | 20 | 2.43% | 11.64% | 13.06% |
| 200 | 10 | 0.06% | 4.27% | 14.35% |
| 200 | 20 | 1.74% | 10.15% | 18.26% |
| 200 | 40 | 2.76% | 11.09% | 14.85% |

Table 1: Mean of mean overestimated ($\bar{\xi}_+$) and underestimated ($\bar{\xi}_-$) prediction errors

905 40, for which overestimated $\bar{\xi}_+ = 2.76\%$ and underestimated $\bar{\xi}_- = 11.09\%$.
906 For the same value of N and the lower value 10 for \bar{r} , overestimated $\bar{\xi}_+$
907 and underestimated $\bar{\xi}_-$ are only 0.06% and 4.27%, respectively. It happens
908 because when peers offer fewer resources, there is more contention in the
909 grid. Since the prediction model assumes that the grid has high contention,
910 the model is more accurate when \bar{r} is low. The first and the third rows of the
911 table show that when $\bar{r} = 20$, the values of overestimated and underestimated
912 errors are larger for larger values of N . This is because the prediction model
913 makes an error in estimating the amount of resources available from each
914 peer, and (as can be seen from the fifth column) more often makes negative
915 than positive errors. As a result, the sum of the errors in the estimate for
916 each peer is larger when the number of peers is larger. From the fifth column,
917 we can see that the frequency of overestimated errors lies between 13% and
918 19% for each of the pairs of values for N and \bar{r} simulated. This result is
919 relevant to situations in which overestimating the amount of resources to be
920 obtained from the grid has worse consequences than underestimating this
921 amount: one such situation is the contract planning presented in this paper.

922 Figure 5 shows all prediction errors ξ for each value of Δt in all simu-
923 lated scenarios. In addition to the errors, the figure also shows the mean
924 of positive errors (overestimations) and negative errors (underestimations),
925 with confidence interval bars for a 95% confidence level. It can be seen that
926 most of the prediction errors ξ are negative for all scenarios. It is due to the
927 pessimistic estimation made by the prediction model, which considers that
928 overestimating is worse than underestimating for most of the cases, including
929 the application presented in this paper. Moreover, the longer the prediction
930 time interval is, the more accurate the prediction tends to be. We think
931 the reason for this is as follows. When a peer is consuming, the balances
932 that other peers record for it decrease until either they reach zero or the
933 peer finishes consuming. When all these balances are zero, the peer can only

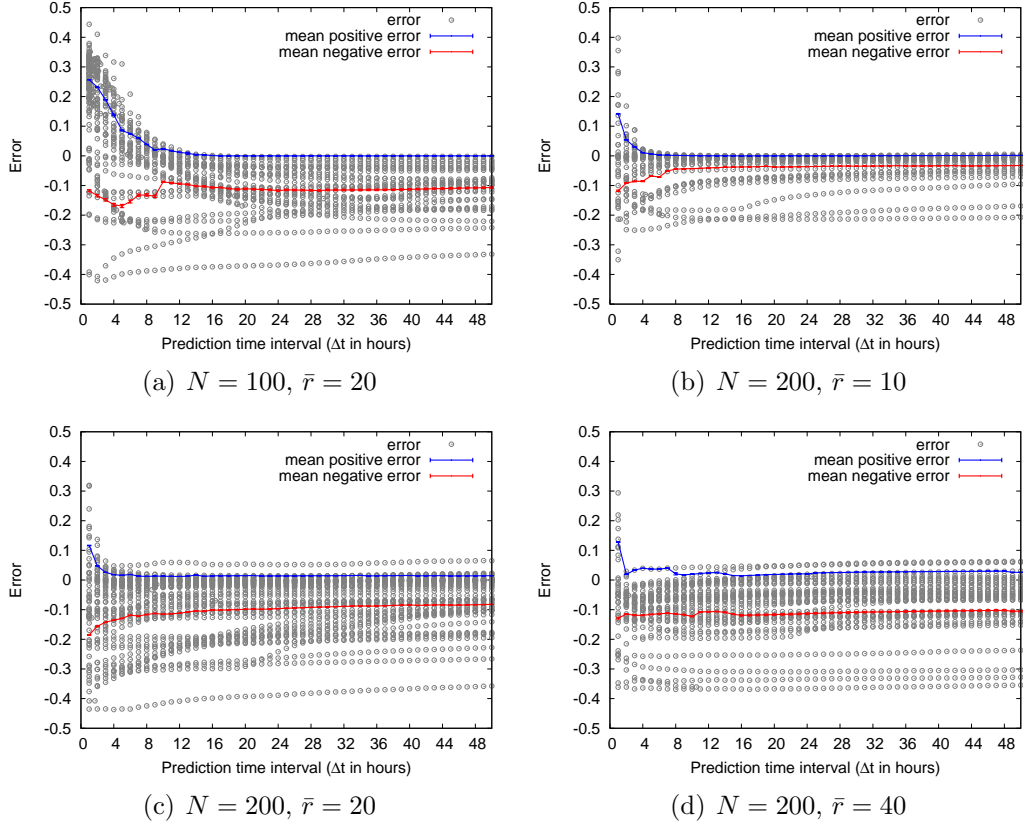


Figure 5: Absolute error values ξ , mean overestimated prediction errors ($\bar{\xi}_+$) and underestimated prediction errors ($\bar{\xi}_-$) for different prediction time interval sizes ($\Delta(t)$ in hours).

934 obtain resources from altruistic peers. Since the amount of resources it re-
 935 ceives from altruistic peers does not change much over time, the model can
 936 estimate this value more accurately than the amount of resources received
 937 from non-altruistic peers, and so the model makes more accurate predictions
 938 in cases where consuming peer's balance is zero for a long period of time.

939 We now retrofit the prediction given by this model in the *Predictive*
 940 heuristic presented in Section 5. For a given grid prediction model, the
 941 average efficiency of the *Predictive* heuristic can be expressed as:

$$p \cdot \mathcal{E}_{\text{Predictive}}(\bar{\xi}_+) + (1 - p) \cdot \mathcal{E}_{\text{Predictive}}(\bar{\xi}_-),$$

942 where $\mathcal{E}_{\text{Predictive}}(\xi)$ is the efficiency of the heuristic for an error ξ , p is the

943 probability of the prediction model overestimate the amount of resources to
 944 be received within a given time interval, and $\bar{\xi}_+$ (resp. $\bar{\xi}_-$) is the average
 945 overestimation (resp. underestimation) error.

946 For the *AoN* application, the prediction is made for a 12-hour interval.
 947 From our assessment, in this case, the grid model proposed has $\bar{\xi}_+ = 1\%$
 948 and $\bar{\xi}_- = 9\%$, leading to an average efficiency of 96.69% in the worst case
 949 ($N = 200$ and $\bar{r} = 20$). On the other hand, the *GDuD* application has
 950 running times of less than two hours. In this case, $\bar{\xi}_+ = 16\%$ and $\bar{\xi}_- = 14\%$
 951 which gives a worst case efficiency of 90.05%.

952 8. Conclusion

953 In this paper we have extended our previous research on business-driven
 954 management of a hybrid IT infrastructure [11], reporting extended models
 955 and new results on this topic. We believe that this work will assist the owners
 956 of IT infrastructures, by providing business-driven heuristics to decide when
 957 to use in-house resources, when to use P2P grid resources, and when to
 958 reserve resources from cloud computing providers.

959 A. Summary of Principal Notation

| Symbol | Meaning |
|-----------------------|------------------------------------------------------------------------|
| Δ | Time interval within which application should be executed; |
| \mathcal{A} | Application to be executed; |
| w | Application's processing demand in cycles; |
| t_r | Time the application is ready for execution; |
| $u(t)$ | Application's utility function; |
| t_d | Deadline for the application; |
| t_c | Time the application is completed; |
| $i(t)$ | # cycles available at time t from in-house infrastructure; |
| $g(t)$ | # cycles available at time t from P2P grid; |
| $p(t)$ | # cycles available at time t from cloud computing provider; |
| \mathcal{K} | Contract between customer and cloud computing provider; |
| $t_e^{\mathcal{K}}$ | Time at which the contract is established; |
| $t_u^{\mathcal{K}}$ | Time at which the cycles will be used; |
| $c_r^{\mathcal{K}}$ | # cycles reserved under contract \mathcal{K} ; |
| $\beta^{\mathcal{K}}$ | Variable reflecting the relative costs of reservation and consumption; |

| | |
|---------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------|
| $\gamma_p^{\mathcal{K}}(c)$ | Cost of contract \mathcal{K} for consuming c of the reserved cycles; |
| \mathcal{P} | The plan (set) of established contracts; |
| $Profit(\mathcal{A}, \Delta, \mathcal{P}, \mathcal{U})$ | Profit from executing application \mathcal{A} , within Δ , under plan \mathcal{P} , with usage log \mathcal{U} ; |
| $\gamma_i(\Delta)$ | Cost of maintaining the dedicated in-house infrastructure; |
| $\varphi(t_e^{\mathcal{K}}, t_u^{\mathcal{K}})$ | Function reflecting how the reservation fee per cycle varies with the urgency of the contract; |
| v_i | Fixed cost of each cycle available on the in-house infrastructure; |
| v_p | Cost of reserving a cycle from the provider at t_p and consuming it just before t_d ; |
| $c_u^{\mathcal{K}}$ | # cycles consumed under contract \mathcal{K} ; |
| $[t_s, t_f]$ | Time period over which the grid's behaviour is predicted; |
| b_k^i | Balance that peer p_i associates with peer p_k ; |
| p_0 | The local peer; |
| $b_0(t)$ | Estimated aggregated balance of the local peer on all donating peers at time t ; |
| N | Number of peers in the grid other than the local peer; |
| \bar{r} | Mean amount of resources provided by a donating peer; |

Table 2: Summary of Principal Notation.

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